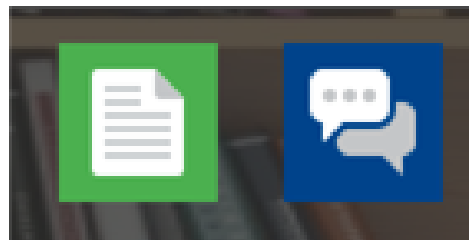


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# Math Resource Fixer-Uppers

Core Advocates Monthly Webinar  
May 6, 2020



STUDENT  
ACHIEVEMENT  
PARTNERS

The webinar will begin shortly. Check your Resource widget to preview the resources for today's session! Use the Group Chat to introduce yourself!

# Introductions

## Your hosts from Student Achievement Partners:

***Pascale Joseph***  
*Project Coordinator,  
Tools and Classroom Resources, SAP*



## This month's presenters:

***Jason Zimba***  
*Founding Partner  
Student Achievement Partners*



***Elizabeth Meier***  
*Innovation Development Manager  
Student Achievement Partners*



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# How many Core Advocate Webinars have you attended?

Please use the Questions tab on your control panel to respond.

If using a poll, please put up to 5 answer choices in the notes section below and indicate if attendees should choose only one response or multiple responses.

# Join Our Network!

[www.achievethecore.org/ca-signup](http://www.achievethecore.org/ca-signup)

ACHIEVE THE CORE

Professional Learning ▾

Planning & Reflection ▾

Classroom Resources ▾



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## National Core Advocate Network

College- and career-ready standards, including the CCSS, give educators an opportunity to work together and support each other— across districts, states, and content areas. The goal of the Core Advocates Network is to engage educators with the content knowledge and resources they need to support teachers and students in the transition towards a college- and career-ready education.

### Join the Network

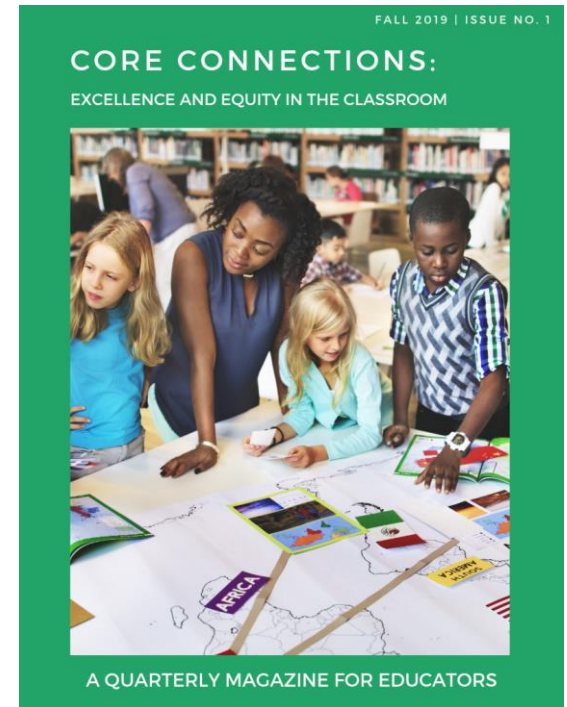
Interested in joining the Core Advocate network? Start by taking the

[Core Advocates Survey](#)

core advocates ►

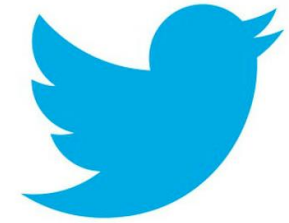
# Learn More About Us!

- Contact Jennie Beltramini ([jbeltramini@studentsachieve.net](mailto:jbeltramini@studentsachieve.net) )  
Joy Delizo-Osborne ([jdelizo-osborne@studentsachieve.net](mailto:jdelizo-osborne@studentsachieve.net))
- Complete this survey to join our database (and mailing list):  
[www.achievethecore.org/ca-signup](http://www.achievethecore.org/ca-signup)
- Visit our website:  
[www.achievethecore.org](http://www.achievethecore.org)



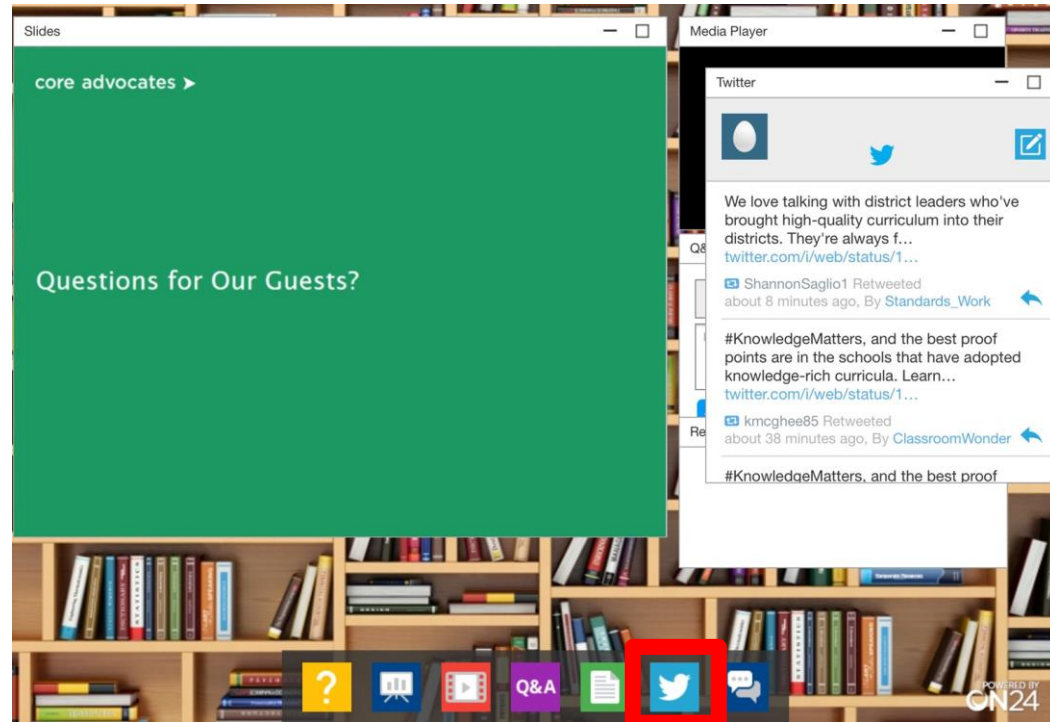
Free, ready-to-use classroom resources  
that support excellent, standards-aligned  
instruction for all students

# Tweet with Us!



Please feel free to tweet during and after the webinar using #coreadvocates

- @achievethecore
- @JennieBeltro



Click here!



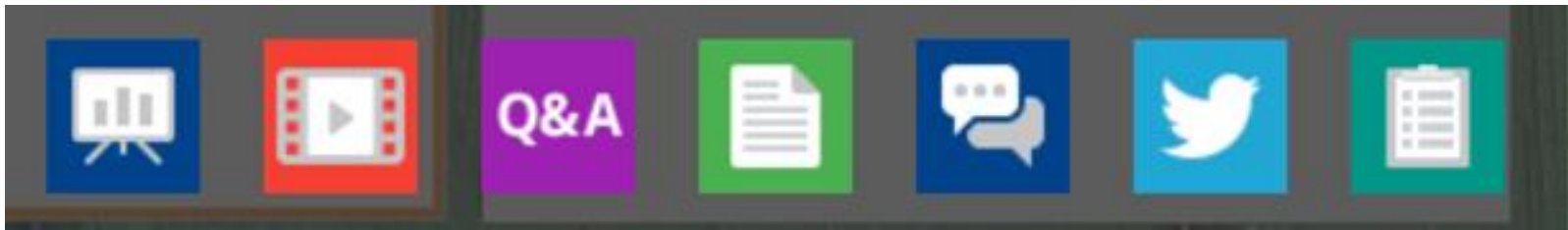
# Engage with Us!

During the webinar:

Question just for  
the presenters/ tech  
help

Resources

Group chat



After the webinar:

- Access to recording will be emailed to you.

*Take our survey in 2 weeks and receive a certificate verifying 1 hour of professional learning.*

# Agenda

## Introduction

The game of “Good Thing, Bad Thing, Change One Thing”

Some ways to make improvements

Q&A

Next steps

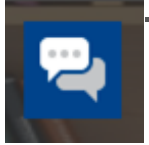


# In what grades do you work with students and/or teachers on mathematics?

Please use the Questions tab on your control panel to respond.

If using a poll, please put up to 5 answer choices in the notes section below and indicate if attendees should choose only one response or multiple responses.

# Norms for our time together



- **Use the group chat** to think out loud, comment on each other's thinking, ask follow-up questions for Liz & myself to elevate. By the end, our list of chat comments should look like a transcript of a productively noisy classroom.
- Your questions and voices are welcome. Your curiosity and learning are valued. You can feel safe taking risks.
- We (all of us participating today) will promote each other's positive views of student capabilities and high expectations for all students. We will value instruction that responds to and respects the value of all students' backgrounds, languages, cultures, points of view, knowledge, and skills.
- We will think critically about and respond to how representation of multiple perspectives and identities are evident in instructional materials, taking action when materials are lacking in representation.
- **Please use the group chat (say, with a thumbs-up or the like) to let us know you can embrace our norms for today!**

# Agenda

Introduction

**The game of “Good Thing, Bad Thing, Change One Thing”**

Some ways to make improvements

Q&A Session

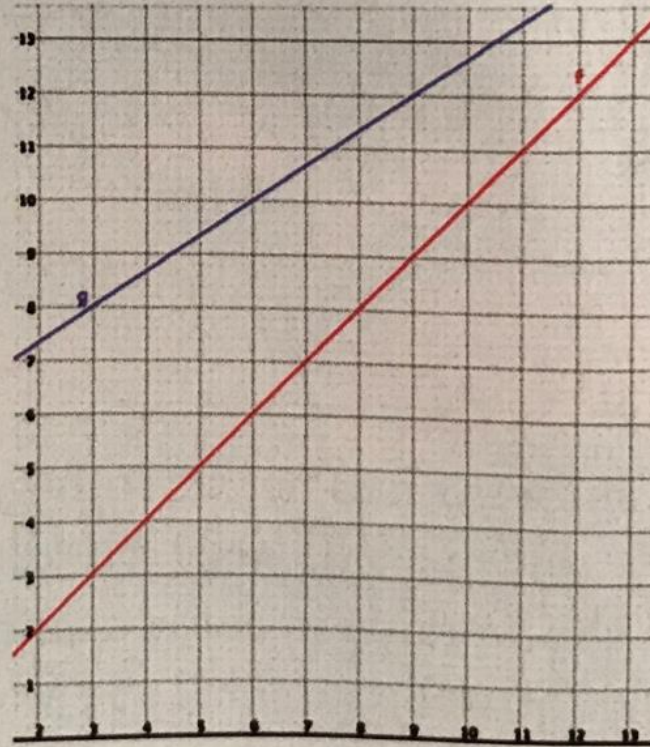
Next steps

# “Good Thing, Bad Thing, Change One Thing”

## How It Works

## Good Thing, Bad Thing, Change One Thing: How It Works

**10.** If the two lines in the graph below continue increasing at a constant rate, at what  $x$ -value will they intersect? (Notice, the  $x$ - and  $y$ -axes are not included in the graph.)



# Good Thing, Bad Thing, Change One Thing: Your Turn!

# Good Thing, Bad Thing, Change One Thing: Your Turn!

We'll show an image of an assignment

Take as much as 5 minutes to read it, do some of the problems

Then start chatting out your Good thing – Bad thing – Change One Things for this assignment as a whole

“Good - ...”

“Bad - ...”

“Change - ...”

Jason will watch the chat and take notes to “comment on the comments”



# Good, Bad, Change One Thing: Your Turn!

Take as much as 5 minutes to read, perhaps do some of the problems



Then use the group chat to start chatting out:

“Good thing - ...”

“Bad thing - ...”

“Change - ...”

## 6.2: Exponent Product Rule

1. Complete the table to explore how to combine two bases that have the same exponent. Use the “expanded” column to work out how to combine the factors into a new base.

expression	expanded	exponent
$5^3 \cdot 2^3$	$(5 \cdot 5 \cdot 5) \cdot (2 \cdot 2 \cdot 2) = (2 \cdot 5)(2 \cdot 5)(2 \cdot 5) = 10 \cdot 10 \cdot 10$	$10^3$
$3^2 \cdot 7^2$		$21^2$
$2^4 \cdot 3^4$		
		$15^3$
		$30^4$
$2^4 \cdot x^4$		
$a^n \cdot b^n$		
$7^1 \cdot 2^4 \cdot 5^4$		

2. What happens if the exponents are not the same? Can you write  $2^3 \cdot 3^4$  with a single exponent? Explain or show your reasoning.

Good thing , Bad thing,  
Change One Thing:  
Your Turn!

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# Agenda

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Name: \_\_\_\_\_

## Hundreds, Tens and Ones

a.  $234 =$  \_\_\_\_\_ hundreds, \_\_\_\_\_ tens, \_\_\_\_\_ ones

b.  $809 =$  \_\_\_\_\_ hundreds, \_\_\_\_\_ tens, \_\_\_\_\_ ones

c.  $571 =$  \_\_\_\_\_ hundreds, \_\_\_\_\_ tens, \_\_\_\_\_ ones

d.  $160 =$  \_\_\_\_\_ hundreds, \_\_\_\_\_ tens, \_\_\_\_\_ ones

e.  $67 =$  \_\_\_\_\_ hundreds, \_\_\_\_\_ tens, \_\_\_\_\_ ones

f. \_\_\_\_\_ = 3 hundreds, 4 tens, 8 ones

g. \_\_\_\_\_ = 6 hundreds, 0 tens, 2 ones

h. \_\_\_\_\_ = 0 hundreds, 0 tens, 5 ones

i. \_\_\_\_\_ = 0 hundreds, 7 tens, 0 ones

j. \_\_\_\_\_ = 9 hundreds, 9 tens, 9 ones



Name: \_\_\_\_\_ Date: \_\_\_\_\_

Make true equations. Write one number in every space. Draw a picture if it helps.

1)  $1 \text{ hundred} + 4 \text{ tens} =$  \_\_\_\_\_

2)  $4 \text{ tens} + 1 \text{ hundred} =$  \_\_\_\_\_

3)  $14 \text{ tens} =$  10 tens + \_\_\_\_\_ tens  
= \_\_\_\_\_ hundred + 4 tens  
= \_\_\_\_\_

4)  $7 \text{ ones} + 5 \text{ hundreds} =$  \_\_\_\_\_

5)  $8 \text{ hundreds} =$  \_\_\_\_\_

6)  $106 =$  1 hundred + \_\_\_\_\_ tens + \_\_\_\_\_ ones

7)  $106 =$  \_\_\_\_\_ tens + \_\_\_\_\_ ones

8)  $106 =$  \_\_\_\_\_ ones

9)  $90 + 300 + 4 =$  \_\_\_\_\_

Are these comparisons true or false?

10)  $2 \text{ hundreds} + 3 \text{ ones} > 5 \text{ tens} + 9 \text{ ones}$  \_\_\_\_\_

11)  $9 \text{ tens} + 2 \text{ hundreds} + 4 \text{ ones} < 924$  \_\_\_\_\_

12)  $456 < 5 \text{ hundred}$

From [www.achievethecore.org](http://www.achievethecore.org)

<https://achievethecore.org/page/862/under-standing-place-value-within-1000-mini-assessment>

## Some ways to make (small, gradual) improvements

- Challenge your students
- But don't complicate what is simple
- Refine over time
- What are your students interested in?
- Know the *good* sources of problems, worksheets, resources
- In HS, Blend middle-grades math applications into assignments
- Keep a math problem notebook, or scrapbook

# Challenge your students

“Children prefer mathematical learning experiences that challenge their thinking and allow them to be creative in solving problems, responding positively to statements, such as, ‘I like complex problems more than easy problems’ and ‘I like activities that challenge my thinking abilities.’”

*Catalyzing Change in Early Childhood and Elementary Mathematics:  
Initiating Critical Conversations (NCTM, 2020)*

**3A** *Time: 3 minutes*

Together Jake and Emily have 20 CDs. Emily has 2 more CDs than Jake. What is the number of CDs that Jake has?

**1A** *Time: 3 minutes*

What is the value of the following?

$$40 \times 30 \times 20 \times 10 \div 20 \div 40 \div 6$$



Which is greater?  $0 + 0 + 0 + 0 + 0 + 0 + 0 + 0 + 50 + 0 + 0$   $20 + 10 + 10$

(JZ)

### Which is greater?

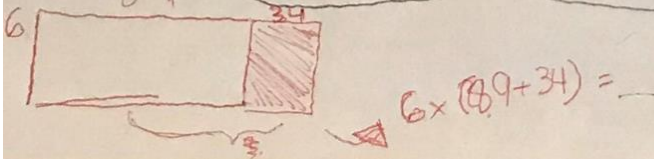
In each case, circle the greater quantity. Do not calculate anything. If the two quantities are equal, circle them both.

$2,329,098 + 10$	$2,329,098 + 11$
$3,785 + 2,817$	$2,817 + 3,785$
$538 - 17$	$538 - 10 - 6$
$538 + 88 - 88$	$538 - 44 + 44$
$89 + 34$	$90 + 33$

### Which is greater?

In each case, circle the greater quantity. Do not calculate anything. If the two quantities are equal, circle them both.

$8,198$	$3 \times 8,198$
$8,198$	$1 \times 8,198$
<del><math>6 \times (89 + 34) - 6 \times 34</math></del>	$6 \times 90$
$6 \times (89 + 34)$	$6 \times (90 + 33)$



### Which is greater?

In each case, circle the greater quantity. Do not calculate anything. If the two quantities are equal, circle them both.

$637 \times 322$	$322 \times 637$
$637 \times 3 \div 3$	$3 \times 637 \div 3$
$637 \times 32 \div 31$	$32 \times 637 \div 32$
$21 \div 4$	$20 \div 4$
$1,287 \div 17$	$1,287 \div (2 \times 17)$

### Which is greater?

In each case, circle the greater quantity. Do not calculate anything. If the two quantities are equal, circle them both.

$2/3 \times 1/8$	$1/8 \times 2/3$
$4 \times 3/5 \div 3/5$	$3/5 \times 4 \div 3/5$
$637 \times 1/3$	$637 \times 1/5$
$6 \times (8/9 + 3/4)$	$6 \times (3/4 + 8/9)$
$3/3 \times 8/8$	$9/9$

(JZ)

Start with 256. At each step, divide by 2. Repeat forever!

a) Show 4 steps of the <sup>(sequence)</sup> pattern.

256, 128, 64, 32

b) Prove or disprove: every number in this <sup>(sequence)</sup> pattern is a whole number.

256, 128, 64, 32, 16, 8, 4, 2, 1,  
~~1/2, 1/4, 1/8, 1/16, 1/32, 1/64, 1/128, 1/256...~~

It's false that every number in this pattern is a whole number because eventually the numbers turn into ~~fractions, or~~ fractions less than 1.

Also,  $1/2$  is part of the pattern, so that's another way to prove that it's false.

(JZ)



# Polygons

1. How many sides does an octagon have?

8

2. How many angles does a triangle have?

3

3. Does a rectangle have more sides or angles?

same

4. How many sides does a pentagon have?

5

5. Which has more sides: a hexagon or a pentagon?

hexagon

6. How many pairs of parallel lines does a trapezoid have?

at least 1

7. How many pairs of parallel lines does a square have?

2

8. How many pairs of parallel lines does a triangle have?

0

9. What polygon has 6 sides and 6 angles?

hexagon

10. Name four types of quadrilaterals.

square, rectangle, rhombus, trapezoid

11. Does a polygon usually have more sides or more angles? Explain.

A polygon usually has <sup>the same</sup> ~~more~~ amount of angles and sides. Every shape has the same

12. Is a cube a polygon? Why or why not?

No, a cube is not a polygon because a polygon is flat, 2D, and a cube is 3D.

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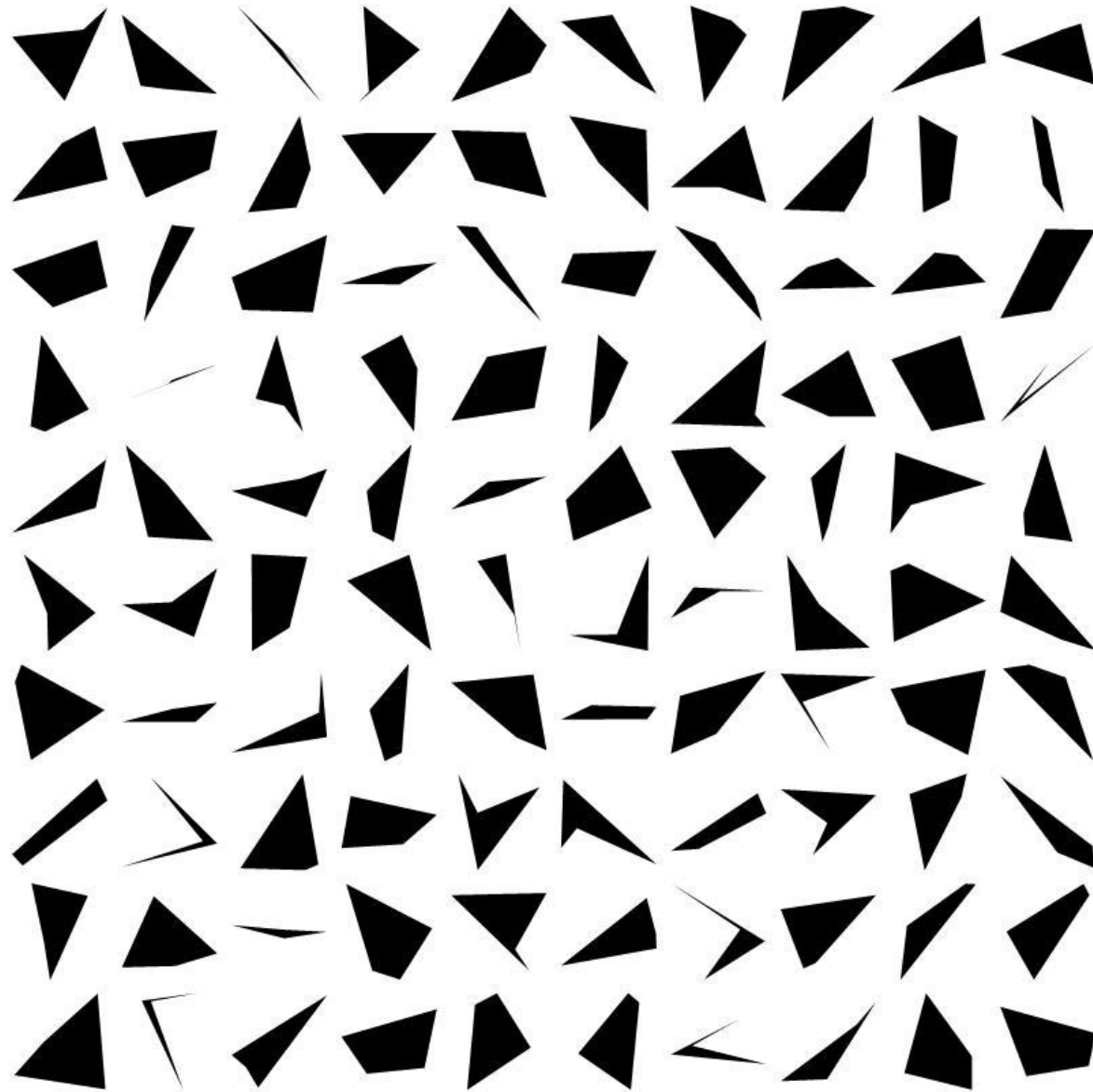
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No, a cube is not a polygon because a polygon is flat, 2D, and a cube is 3D.

If possible, draw a quadrilateral that isn't one of the four types you named.



(JZ)



## Part 1: Math Magic

Here are two math tricks! But the really clever trick is explaining why these tricks are math, not magic! Like all good magicians, you should practice by trying them out. Then, try to explain why they work.

### Math-e-magic #1:

- Think of a number
- Double it
- Add 10
- Halve it
- Take away your original number

Try this with a different starting number. Did you get a different result? Why does this happen?

For both numbers I got 5 as the result. It happens because half of 10 is 5, so after you've doubled it and added 10, when you divide it by two then you just always get 5 more than the original number, so when you subtract, it results in 5.

### Math-e-magic #2:

- Think of a number
- Multiply the number by 3
- Add 8 more than the original number
- Divide by 4
- Subtract the original number

Try this with a different starting number. Did you get a different result? Why does this happen?

I first tried it with 2, then with 10. Each time I got 2 as the result. It happens because once you get to the fourth step, you added 8 more than the original, so when you divide  $[(n \cdot 3) + (n + 8)]$  by 4, you're doing  $[(n \cdot 4) + 8] \div 4$ . The result will be  $[n + (8 \div 4)]$ , which is  $(n + 2)$ , so it will always be 2 when you subtract.

Could you make your own mathematical trick and explain why it works?

Think of a number  
Duplicate it  
Add 9  
Add 3  
Divide it in two  
Subtract the original number  
And you always get 6!

My trick works because you're doing  $(n \cdot 2) + (n + 2) \div 2$ , which is the same as  $(n \cdot 2 \div 2) + (n \div 2)$ , which is  $n + 6$ . So when you subtract  $n$  from  $(n + 6)$ , you always get 6.





Area of a Parallelogram = base  $\cdot$  height

$$\text{Area of a Triangle } \Delta = \frac{1}{2} (\text{base} \cdot \text{height})$$

$$\text{Area of a circle} = \pi \cdot r^2$$

Area of a rectangle = base  $\cdot$  height

Area of a Trapezoid  $\square = \frac{1}{2} \cdot (\text{base 1} + \text{base 2}) \cdot \text{height}$

Area of a semicircle =  $\frac{1}{2} \cdot \pi r^2$

Area of a quarter circle =  $\frac{1}{4} \cdot \pi r^2$

$$SA = LA + 2b$$

$$\text{Volume} = Bh$$


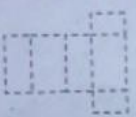

(L  $\cdot$  w)




**Shelbi Cole**

Mar 6, 2017

Grade 2 "enrichment" worksheet. Neighbor's kid says in my car as he is doing this for homework, "we didn't learn this." I guess that's good then. At least your not learning the 6th grade standards and \*only\* doing them for homework.

1.		cube cylinder cone
2.		cube rectangular prism cylinder
3.		cube cone rectangular prism

 **Writing and Reasoning** In Exercise 1, how did you know which shape the faces on the net made?

But don't complicate what is simple

NAME \_\_\_\_\_

If you know the sum, just write it down. If not, then find the sum by making ten.

$$\begin{array}{r} 5 \\ + 9 \\ \hline \end{array}$$

$$\begin{array}{r} 7 \\ + 4 \\ \hline \end{array}$$

$$\begin{array}{r} 6 \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} 8 \\ + 4 \\ \hline \end{array}$$

$$\begin{array}{r} 7 \\ + 6 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ + 4 \\ \hline \end{array}$$

$$\begin{array}{r} 7 \\ + 7 \\ \hline \end{array}$$

$$\begin{array}{r} 3 \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ + 6 \\ \hline \end{array}$$

$$\begin{array}{r} 8 \\ + 3 \\ \hline \end{array}$$

$$\begin{array}{r} 4 \\ + 7 \\ \hline \end{array}$$

$$\begin{array}{r} 6 \\ + 9 \\ \hline \end{array}$$

$$\begin{array}{r} 7 \\ + 5 \\ \hline \end{array}$$

$$\begin{array}{r} 8 \\ + 7 \\ \hline \end{array}$$

$$\begin{array}{r} 2 \\ + 9 \\ \hline \end{array}$$

$$\begin{array}{r} 5 \\ + 7 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ + 9 \\ \hline \end{array}$$

$$\begin{array}{r} 6 \\ + 7 \\ \hline \end{array}$$

$$\begin{array}{r} 8 \\ + 5 \\ \hline \end{array}$$

$$\begin{array}{r} 7 \\ + 9 \\ \hline \end{array}$$

$$\begin{array}{r} 5 \\ + 6 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} 4 \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ + 5 \\ \hline \end{array}$$

$$\begin{array}{r} 8 \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} 8 \\ + 6 \\ \hline \end{array}$$

$$\begin{array}{r} 4 \\ + 9 \\ \hline \end{array}$$

$$\begin{array}{r} 6 \\ + 6 \\ \hline \end{array}$$

$$\begin{array}{r} 5 \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} 3 \\ + 9 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ + 7 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ + 3 \\ \hline \end{array}$$

$$\begin{array}{r} 6 \\ + 5 \\ \hline \end{array}$$

$$\begin{array}{r} 7 \\ + 8 \\ \hline \end{array}$$

$$\begin{array}{r} 8 \\ + 9 \\ \hline \end{array}$$

$$\begin{array}{r} 9 \\ + 2 \\ \hline \end{array}$$

(JZ)



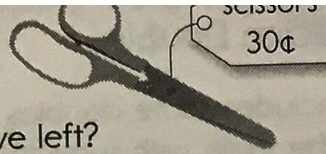
- ⑦ Amanda has 70¢.  
She buys a pair of scissors.  
How much money does she have left?

40 ¢

Write a number model to show how you found the answer. **Sample answers:**

$70 - 30 = 40$ ;  $70 - 30 = \underline{\quad}$

Tell how you could use a number grid to find out how much more. **Sample answer:** I could start at 70, then move down 4 rows to 30. 4 rows is the same as 40.



answer makes sense.

②  $17 + 68 = ?$

Ballpark estimate:

$20 + 70 = 90$

Strategy:

$$\begin{array}{r} 17 \\ + 68 \\ \hline 85 \end{array}$$
  
you add ones to ones, and tens to tens.

$17 + 68 = 85$

above Explain your estimate  
plain how you checked to  
sense

# Calibrating on Fluency

Alongside many other goals, K-5 teaching must endow students with these important procedural fluencies that build steadily across years of schooling:

- Remembering single-digit sums and fluency with related differences
- Remembering single-digit products and fluency with related quotients
- Calculating with paper and pencil using the standard base-ten algorithms
- Calculating mentally using algebraic thinking about numbers



# Calibrating on Fluency

What about grades 6-HS?

Time is used inefficiently if **every** topic is construed as a procedure, and **every** procedure is reinforced to fluency.

Examples:

- Determining the median value of an artificial data set
- Applying volume formulas
- Factoring trinomials over the integers
- Simplifying complex rational expressions

# Mean

Add up all the numbers and divide by the number in the set.

$$\frac{2+2}{2} = \frac{4}{2} = 2$$

$$\frac{3+4+6}{3} = \frac{13}{3} = 4.\bar{3}$$

# Median

Order numbers from least to greatest. Find the number in the middle.

X: 1, 3, 4, 4, 6  
 ↑ Median

X: 2, 3, 4, 5, 6  
 Average these to find median  
 $\frac{3+4}{2} = \frac{7}{2} = 3.5 = \text{median}$

# Mode

The number seen most often in the data set.

1, 1, 1, 1, 2  
 Mode = 1    1, 1, 2, 2, 3  
 - Mode = 1 and 2

Five  
Min:  
LQ  
Med  
UC  
M

# Minimum

Smallest number in data set

1, 2, 3, 4, 5, 6, 7  
 ↑ Minimum

# Range

Maximum - Minimum =

1, 5, 8, 3  
 $8 - 1 = 7$  ← Range  
 ↑ Max    ↑ Min

# Maximum

Largest number in a data set

1, 2, 3, 4, 5, 6, 7  
 ↑ maximum

# Distributive Property

$a(b+c) = ab+ac$

Examples

$7(8+3) = 7(8)+7(3) = 56+21 = 77$

$7(x+3) = 7(x)+7(3) = 7x+21$

# Number Sentence

mathematical statement that gives relationship between 2 expressions that are composed of numbers and operations

Examples:

$3+2=5$   
 ↑ Expression    ↑ Expression  
 operation OR operation

$x+4=6$   
 ↑ Expression    ↑ Expression

# Commutative Property of Multiplication

order of multiplication does not change result (answer)

Examples:  $(6)(8) = 8(6)$   
 or  $-4(-7) = (-7)(-4)$

Find the five-number summary plot for each data set

**61 Monthly Revenue**

7, 10, 10, 12, 13, 13, 14, 14, 15, 16, 16, 17, 18, 18, 19, 19, 20, 20, 20, 20, 21, 21, 22, 23, 23, 24, 25, 25, 26, 26, 27, 27, 28, 29, 29, 30, 30, 31, 31, 32, 32, 33, 34, 34, 35, 35, 36, 37, 37, 38, 39, 40, 41, 42, 43, 44, 45, 45, 46, 47, 48, 49, 50, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100

**62 Mean Height (Centimeters)**

140, 145, 150, 155, 160, 165, 170, 175, 180, 185, 190, 195, 200, 205, 210, 215, 220, 225, 230, 235, 240, 245, 250, 255, 260, 265, 270, 275, 280, 285, 290, 295, 300, 305, 310, 315, 320, 325, 330, 335, 340, 345, 350, 355, 360, 365, 370, 375, 380, 385, 390, 395, 400, 405, 410, 415, 420, 425, 430, 435, 440, 445, 450, 455, 460, 465, 470, 475, 480, 485, 490, 495, 500, 505, 510, 515, 520, 525, 530, 535, 540, 545, 550, 555, 560, 565, 570, 575, 580, 585, 590, 595, 600, 605, 610, 615, 620, 625, 630, 635, 640, 645, 650, 655, 660, 665, 670, 675, 680, 685, 690, 695, 700, 705, 710, 715, 720, 725, 730, 735, 740, 745, 750, 755, 760, 765, 770, 775, 780, 785, 790, 795, 800, 805, 810, 815, 820, 825, 830, 835, 840, 845, 850, 855, 860, 865, 870, 875, 880, 885, 890, 895, 900, 905, 910, 915, 920, 925, 930, 935, 940, 945, 950, 955, 960, 965, 970, 975, 980, 985, 990, 995, 1000

**63 Census per World Series**

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100

**64 Test Scores**

10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80, 85, 90, 95, 100

Can you divide the packages? In each row, determine which set of data has the greatest mean absolute deviation. You may need to use another sheet of paper to record the mean, the deviations from the mean, and the average distance from the mean. Circle the letter next to the greatest mean absolute deviation in each row. The first one has been completed for you.

1	mean = 7, M.A.D. = 1.67	F	M	mean = 17, M.A.D. = 2.47
2	mean = 14, M.A.D. = 0.75	Y	A	mean = 14, M.A.D. = 2.25
3	mean = 100, M.A.D. = 1.0	R	H	mean = 100, M.A.D. = 1.0
4	mean = 100, M.A.D. = 1.2	P	E	mean = 100, M.A.D. = 1.2
5	mean = 10, M.A.D. = 1.3	A	R	mean = 10, M.A.D. = 1.3
6	mean = 10, M.A.D. = 1.2	D	O	mean = 10, M.A.D. = 1.2
7	mean = 100, M.A.D. = 1.0	M	H	mean = 100, M.A.D. = 1.0
8	mean = 10, M.A.D. = 1.0	M	U	mean = 10, M.A.D. = 1.0
9	mean = 10, M.A.D. = 1.0	R	E	mean = 10, M.A.D. = 1.0
10	mean = 10, M.A.D. = 1.0	A	T	mean = 10, M.A.D. = 1.0
11	mean = 10, M.A.D. = 1.0	S	N	mean = 10, M.A.D. = 1.0

Read the instruction book to find out how to use the cracker.

Five Plot and MAD

Homework

Find the mode, median, mean, and mean absolute deviation for each data set.

1. 4 Weeks in Book Titles

A) Mode = 2, Median = 5, Mean = 3.33 and MAD = 1.28  
 B) Mode = 2, Median = 3, Mean = 3.22 and MAD = 1.36  
 C) Mode = 7, Median = 3, Mean = 3.33 and MAD = 1.31  
 D) Mode = 2 and 3, Median = 3, Mean = 2.87 and MAD = 0.81

2. 4 Weeks in Study Cases

A) Mode = 1, Median = 3, Mean = 4 and MAD = 2  
 B) Mode = 5, Median = 5, Mean = 4.89 and MAD = 0.84  
 C) Mode = 1, Median = 5, Mean = 3.89 and MAD = 1.88  
 D) Mode = 6, Median = 6, Mean = 7 and MAD = 1.36

Find the mode, range, lower quartile, upper quartile, and interquartile range for each data set.

1. Test Scores

A) Mode = 12, Range = 22, Q1 = 42, Q2 = 52 and IQR = 10  
 B) Mode = 11, Range = 17, Q1 = 43, Q2 = 51 and IQR = 8  
 C) Mode = 49 and 51, Range = 23, Q1 = 47, Q2 = 51 and IQR = 4  
 D) Mode = 49, Range = 21, Q1 = 41, Q2 = 49 and IQR = 8

2. 4 Weeks in Book Titles

A) Mode = 2, Range = 4, Q1 = 2, Q2 = 7 and IQR = 5  
 B) Mode = 2, Range = 4, Q1 = 2, Q2 = 4 and IQR = 2  
 C) Mode = 2, Range = 3, Q1 = 2, Q2 = 7 and IQR = 5  
 D) Mode = 3, Range = 4, Q1 = 1, Q2 = 4 and IQR = 3

**SAFE CRACKER!**

You are a world famous safe-cracker! After you solve the clues or when people find their combinations, they come to you for help. Use the clues to help crack the safes.

1. The first number is the lower extreme (minimum).

The second number is the range of the data.

The third number is the interquartile range of the data.

The combination is 14 16 8

Now open it up and see the treasure inside!

2. The first number is the upper quartile.

The second number is the lower quartile.

The third number is the interquartile range.

The combination is 97 77 15

Now open it up and see the answers to all the safe's math problems inside!

3. The first number is the lower extreme (minimum).

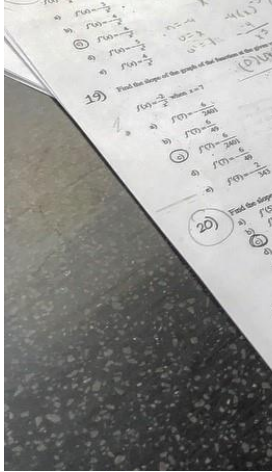
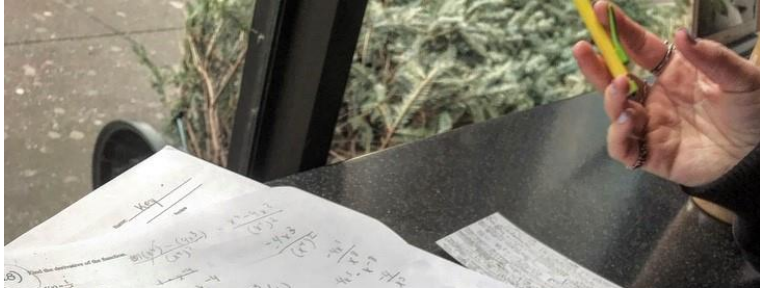
The second number is the interquartile range.

The third number is range.

The combination is 23 22 15

Now open it up and see the treasure!





19) Find the slope of the graph of the function at the given value.  
 $f(x) = \frac{2}{x}$  when  $x = 7$   
 a)  $m = -\frac{2}{49}$   
 b)  $m = -\frac{2}{7}$   
 c)  $m = -\frac{2}{49}$   
 d)  $m = -\frac{2}{7}$

20) Find the slope of the graph of the function at the given value.  
 $f(x) = 2x^2 + 9x + 5$   
 a)  $f'(5) = 59$   
 b)  $f'(5) = 375$   
 c)  $f'(5) = 384$   
 d)  $f'(5) = 259$   
 e)  $f'(5) = 420$

21) Find the vertical asymptotes (if any) of the function  $f(x) = \frac{2-x}{x^2-3x+6}$   
 a)  $x = 2$   
 b)  $x = 3$   
 c)  $x = 1$   
 d)  $x = -6$

Calculations shown:  
 $\frac{(0)(7^2) - (2)(7)(-2)}{7^2}$   
 $\frac{-28}{49} = -\frac{2}{49}$   
 $f'(x) = 4x + 9$   
 $f'(5) = 4(5) + 9 = 20 + 9 = 29$   
 $\frac{(x-1)(x-3)}{(x-3)(x-2)}$   
 $\frac{x-1}{x-2}$

### Part One

Monica and Jose have different methods for finding square roots.

#### Monica's Method

To find the square root of  $x$ , find a number where the product of the number and itself is  $x$ . For example,  $2 \cdot 2 = 4$ , so the square root of 4 is 2.

#### Jose's Method

To find the square root of  $x$ , divide  $x$  by 2. For example,  $4 \div 2 = 2$ , so the square root of 4 is 2.

Which student's method is **not** correct?

Monica's method

Jose's method

Explain why the method you selected is not correct **in complete sentences**.

Jose's method is wrong because you aren't supposed to divide  $x$  by 2 and get 4. You're supposed to multiply 2 times itself, get 4, and the square root is 2.

# Calibrating on Fluency

What about grades 6-HS?

Time is used inefficiently if **every** topic is construed as a procedure, and **every** procedure is reinforced to fluency.

Examples:

- Determining the median value of an artificial data set
- Applying volume formulas
- Factoring trinomials over the integers
- Simplifying complex rational expressions

In cases like the above in grades 6-HS, reams of repetitive “bite-size” problems consume too much time that might instead be spent in

- Fostering student understanding of the topic (which is more durable)
- Providing students with “life-size” problems (meaningful and rewarding)
- Reinforcing procedural fluency where it actually matters (such as distributive property, equation solving)

Refine over time

10. Ninety-seven lunch trays were placed equally in 4 stacks. How many lunch trays will be left over?



\$13.00

14. Ryan transfers 15% of his monthly pay into a savings account. If Max makes \$1850 per month, how much will he save in a year?

$$789 \times 38 - 789 \times 1 = (789 \times 37) \quad 789 \times 38 - 789 \times 15 = (789 \times 23)$$

Easier with the Distributive Property

$$(12 \times 789) - (11 \times 789) = (1 \times 789)$$

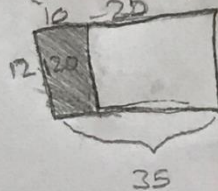
Harriet's notebook had 215 pages. There were 4 mean things and 3 nice things on every page. Did Harriet write more mean things or more nice things?

How many more did Harriet write in all?

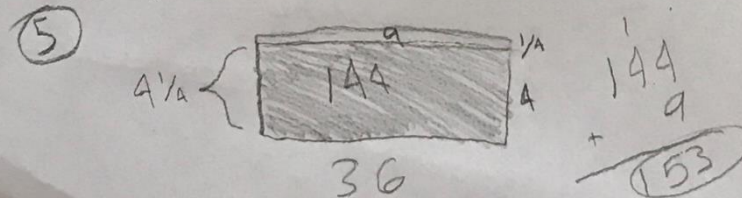
$$\begin{array}{r} 880 \\ - 665 \\ \hline 215 \end{array} \quad \begin{array}{r} 789 \\ + 645 \\ \hline 1505 \end{array} \quad \begin{array}{r} 4 - 3 = 1 \\ 1 \times 215 = 215 \end{array}$$

- ①: No mean things
- ②: 215 more
- ③: Pepper eats 35 kibbles a day. Pearl eats 25 kibbles a day. Each kibble weighs 12 grams. How many more grams does Pepper eat each day?

$$(12 \times 35) - (12 \times 25) = (12 \times 10)$$



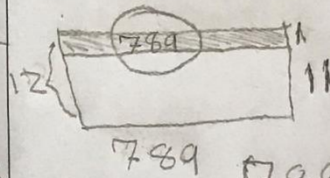
Illustrate the distributive property for one of the above problems.



$$789 \times 12 = ?$$

$$\begin{array}{r} 10 \times 1 \\ 1789 \\ \times 12 \\ \hline 1578 \\ + 7890 \\ \hline 9468 \end{array}$$

$$789 \times 12 - 789 \times 11 = ?$$



$$(789 \times 12) - (789 \times 11) = (789 \times 1)$$

$$4 \frac{1}{2} \times 36 = ?$$

$$\begin{array}{r} 144 \\ + 9 \\ \hline 153 \end{array}$$

$$4 \times (3 \times 12) = (12 \times 12)$$

$$789 \times 38 - 789 \times 1 = (789 \times 37) \quad 789 \times 38 - 789 \times 15 = (789 \times 23)$$

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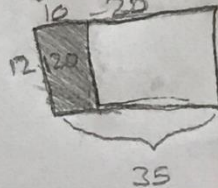
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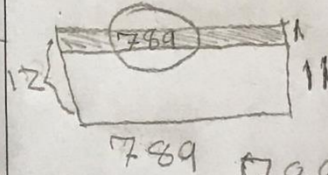
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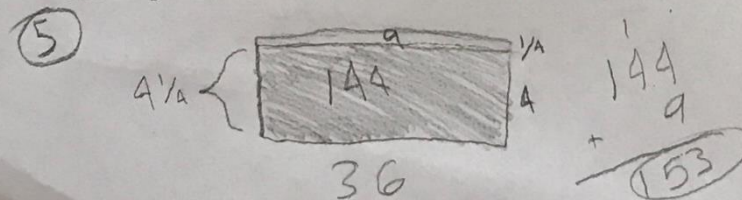
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(JZ)

# Refining Word Problem Assignments

Sometimes, mix it up. Reorder sentences so that the question comes first ... delete the question sentence leaving just the “givens” and ask the student to create a question and answer it ... ask a qualitative question (‘I spent 40% of a 12-hour trip playing video games. Was that more or less than 6 hours of video games?’)

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Delete “explain” or “justify” for word problems. Instead...

For one-step word problems:

- Mostly, just pose the problem, giving space to show work. Can say something like, “Draw a diagram if it helps.”
- Sometimes, pose the problem and ask for an equation involving an unknown number. Can say something like, “Write an equation that you could solve to find the answer.” (Don’t really need to ask for the answer in this case.)
- Don’t bother asking for a writeup in words about a one-step word problem.

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Write a note to a classmate describing what your solution plan was.  
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- ⑥ Nathan has 5 bags of marbles.  
Each bag has 4 yellow marbles and 6 red marbles.

How many marbles does Nathan have in all?

The letter  $M$  represents the number of marbles that Nathan has.

- a. Underline the number model that fits the story.

$$5 \times 4 + 6 = M$$

$$\underline{5 \times (4 + 6) = M}$$



$$(5 + 4) \times 6 = M$$

What are your students interested in?

# Why do basketball players love doughnuts?

Name \_\_\_\_\_

Solve and show your work. Place the letter of the problem in the blank above the numerical answer at the bottom of the page. Use 3.14 for pi and round answers to the nearest whole number as necessary.



<p>N)</p>	<p>M)</p>	$V_{\text{pyramid or cone}} = \frac{1}{3} Bh$ <p>B: Base Area h: height</p>
<p>Y)</p>	<p>D)</p>	<p>C)</p>
<p>T)</p>	<p>E)</p>	<p>U)</p>
<p>A)</p>	<p>H)</p>	<p>K)</p>



On Mindset and Practices for  
Re-Integrating "Belonging" into  
Mathematics Instruction

J. Sharif Matthews

Montclair State University

[http://www.teachingworks.org/images/files/TeachingWorks\\_Matthews.pdf](http://www.teachingworks.org/images/files/TeachingWorks_Matthews.pdf)

Prof. J. Sharif Matthews: 4Hs of belonging-centered math instruction: Home, Hobbies, Hopes, and Heritage.

“For teachers who have begun to develop critical awareness, but don’t know where to begin **integrating students’ culture into mathematics instruction**, I offer this heuristic the 4Hs of belonging-centered math instruction: Home, Hobbies, Hopes, and Heritage. This heuristic offers four locales of meaningful connection for students. Home refers to consistent activities engaged at home or the properties of the home space (e.g., cooking, interactions with family, the heating bill, dimensions of the living room). Hobbies are personal activities engaged in at least once per week (e.g., sports teams, social media, work, smart phone apps/games). Hopes are personal aspirations, interests, or goals (e.g., desired career or major, making the varsity team, making my paycheck last all week). Heritage is a connection to a tradition or a people that is a source of pride (e.g., local celebrities in the community, Black female mathematicians).

## High school teachers: Blend middle-grades math applications into assignments

Suppose that life exists everywhere on Earth to within a depth of 10 miles, but not deeper than that. What percentage of Earth's volume contains life? Try to draw an accurate scale diagram of a cross section of Earth showing the 'living region.'

(JZ)

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# High school teachers: Blend middle-grades math applications into assignments

d	<b>Applying Key Takeaways from Grades 6–8**</b>
tant gory able           n thin	<p><b>Solving problems at a level of sophistication appropriate to high school by:</b></p> <ul style="list-style-type: none"> <li>• Applying ratios and proportional relationships.</li> <li>• Applying percentages and unit conversions, e.g., in the context of complicated measurement problems involving quantities with derived or compound units (such as mg/mL, kg/m<sup>3</sup>, acre-feet, etc.).</li> <li>• Applying basic function concepts, e.g., by interpreting the features of a graph in the context of an applied problem.</li> <li>• Applying concepts and skills of geometric measurement e.g., when analyzing a diagram or schematic.</li> <li>• Applying concepts and skills of basic statistics and probability (see 6-8.SP).</li> <li>• Performing rational number arithmetic fluently.</li> </ul>
<small>ing in the domain G-SRT, "Prove theorems using similarity" (pp. 77 c</small>	

<https://achievethecore.org/page/701/widely-applicable-prerequisites-for-college-and-careers>

<https://achievethecore.org/coherence-map/HS/M/tasks>  
(some A1/M1 tasks)

A programmer is writing a piece of software. One part of the software will ask the CPU to repeatedly calculate the value of

$$x * x + 4 * x * y + 3 * y * y.$$

Suppose the CPU can perform  $2.6 \times 10^9$  additions per second, but only  $1.1 \times 10^9$  multiplications per second.

- a) How can the programmer rewrite the expression so that evaluating the expression takes less time? Explain intuitively why your form of the expression evaluates faster.
- b) By rewriting the expression the way you did, what percentage decrease did you achieve in the time required to evaluate the expression?

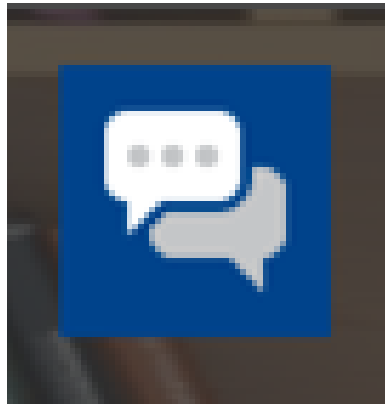
(JZ)



Know the good sources for problems, worksheets,  
resources

Know the good sources for problems, worksheets,  
resources

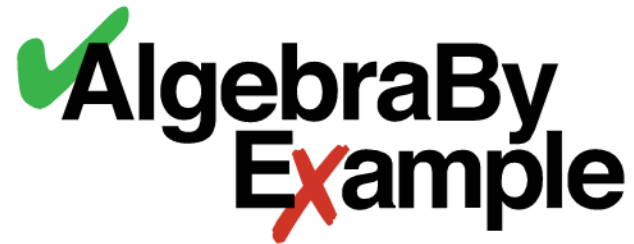
What are your faves?  
Share your answers in the group chat!  
(Free is best!)



Algebra by Example, <https://www.serp institute.org/algebra-by-example>



Who W



AlgebraByExample Home



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The Format

Assignment Topics

The R&D

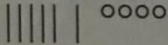
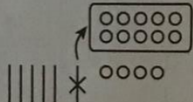
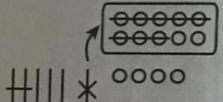
# Powerful Algebra 1 Teaching Strategy

Example-based Problem Sets for Algebra 1

Keep a math problem notebook, or scrapbook

► Explain the **Ungroup First Method**

Mrs. Green likes this method. Explain what she does.

Step 1	Step 2	Step 3
$\begin{array}{r} 64 \\ - 28 \\ \hline \end{array}$	$\begin{array}{r} 514 \\ \cancel{64} \\ - 28 \\ \hline \end{array}$	$\begin{array}{r} 514 \\ \cancel{64} \\ - 28 \\ \hline 36 \end{array}$
		

► Try the Ungroup First Method

Show your work numerically and with a proof drawing.

4. 
$$\begin{array}{r} 42 \\ - 19 \\ \hline \end{array}$$

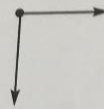
5. 
$$\begin{array}{r} 75 \\ - 46 \\ \hline \end{array}$$

6. 
$$\begin{array}{r} 81 \\ - 37 \\ \hline \end{array}$$

Name each angle. Write acute, obtuse, or right.



\_\_\_\_\_



\_\_\_\_\_



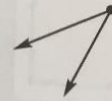
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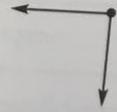


\_\_\_\_\_



\_\_\_\_\_

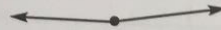
Estimate the size of each angle in degrees.



\_\_\_\_\_



\_\_\_\_\_



\_\_\_\_\_



\_\_\_\_\_

Draw an angle for each of the following measures.

about 10 degrees

about 90 degrees

about 175 degrees



## DIVISION OF WHOLE NUMBERS

### Dividing Larger Numbers with Remainders

divisor: 6

dividend: 3,772

quotient: \_\_\_\_\_

remainder: \_\_\_\_\_

$$6,031 = (q \times 9) + r$$

$$q = \underline{\hspace{2cm}}$$

$$r = \underline{\hspace{2cm}}$$

$$7 \overline{) 1,504}$$

$$1,129 = (q \times 3) + r$$

$$q = \underline{\hspace{2cm}}$$

$$r = \underline{\hspace{2cm}}$$

example

How do you rename  $\frac{2}{5}$  to a decimal?

*Step 1: Rename  $\frac{2}{5}$  to a fraction with a denominator of 10, 100, or 1,000.*

$$\frac{2}{5} = \frac{4}{10}$$

*Step 2: Rename  $\frac{4}{10}$  to a decimal.*

$$\frac{4}{10} = .4$$

Rename to a decimal.

$$\frac{4}{5} = \underline{\hspace{2cm}}$$

$$\frac{7}{20} = \underline{\hspace{2cm}}$$

$$\frac{1}{4} = \underline{\hspace{2cm}}$$

$$\frac{5}{8} = \underline{\hspace{2cm}}$$

$$\frac{3}{4} = \underline{\hspace{2cm}}$$

$$\frac{4}{25} = \underline{\hspace{2cm}}$$

There is a secret in finding which fractions can be renamed directly to decimals.  
Circle the fractions which can be renamed directly to decimals.

$$\frac{2}{3}$$

$$\frac{1}{5}$$

$$\frac{9}{20}$$

$$\frac{1}{6}$$

$$\frac{5}{7}$$

$$\frac{9}{25}$$

My secret is \_\_\_\_\_

\_\_\_\_\_

Example

Commutative Property

$$a \times b = b \times a$$

*Changing the order of the factors does not change the product.*

Associative Property

$$a \times (b \times c) = (a \times b) \times c$$

*Changing the grouping of the factors does not change the product.*

Distributive Property

$$6 \times 17 = (6 \times 10) + (6 \times 7)$$

*You can find a product by renaming one factor as the sum of two addends, multiplying each addend by the other factor, and adding the partial products.*

Identity Property (Property of 1)

$$n \times 1 = n$$

*When 1 is one of two factors, the product is the other factor.*

Property of Zero

$$n \times 0 = 0$$

*When 0 is a factor, the product is 0.*

Tell which property goes with each problem, write an equation, and explain your answer.

In which box will George be able to fit more CD's, a box with 6 rows and 4 CD's in each row, or a box with 4 rows and 6 CD's in each row?

---

---

---

---

Juan has  
with 9 r

Lisa b  
in the

Mol  
she

Ji  
b  
t

Juan has one CD box with 9 rows and 10 CD's in each row. He has another CD box with 9 rows and 6 CD's in each row. How many CD's does Juan have?

Lisa bought a CD rack that has one column which holds 24 CD's. How many CD's are in the rack when it is full?

Molly selected 14 CD's but decided to not buy any of them. How many CD's did she buy?

Jim built two solid figures from 1-inch cubes. One figure has a height of 3 inches and a base that is 5 inches by 2 inches. The other figure has a height of 5 inches and a base that is 2 inches by 3 inches. Which figure is made up of more cubes?

14) Show that the sum of any  $2n + 1$  consecutive integers is divisible by  $2n + 1$ .

(fix a value)

6.)  $10^{n+1} + 10^n + 1$  is divisible by 3.

1.) Find  $f(x) - f(x - 1)$  if  $f(x) = 2x + 3$ .

2.) Find  $f(a) - f(a - 1)$  if  $f(x) = mx + b$ .

5.)  $x^2(a + b) + y^2(a + b)$

33.) 
$$\frac{1}{1 - \frac{1}{2 - \frac{1}{3 - x}}}$$

3.) 
$$\frac{\frac{a+1}{a-1} - \frac{a-1}{a+1}}{\frac{a+1}{a-1} + \frac{a-1}{a+1}}$$

21.) In what range of values must the sum of a real number and its reciprocal lie?

22.) For the equation  $ax^2 + bx + c = 0$  show that

(a) if one root is the negative of the other, then  $b = 0$ ;

16.) Find the maximum value of the product of two numbers, if their sum is 4.

17.) Find the minimum value of the product of two numbers, if their difference is 4.

20.) 
$$\left[ \frac{1}{1-x} - \frac{1}{1+x} \right] + \left[ \frac{1}{1-x} + \frac{1}{1+x} \right]$$

19.) 
$$\frac{(x-y)^2}{y^2 - xy}$$

10)  $\frac{a^4 - b^4}{(a-b)^2} \cdot \frac{a-b}{a^2+ab} \cdot \frac{a^2}{a^2+b^2}$  If  $f(x) = 3x^2 - 4x + 1$  and  $F(x) = x^2 + 6x - 7$ , prove that: (3)  $f(4) = F(4)$

37)  $cx + dy - dx - cy$

27. A takes 2 hr longer than B to walk  $d$  miles, but if A should double his speed, he would walk it in 1 hr less. Find the time B needs to walk the  $d$  miles.

21. What expression must be subtracted from  $x^2 + 2xy + 3y^2$  to give  $x^2 - 3xy - 5y^2$ ?

20. What expression must be added to  $3a - 4b + 6c$  to give  $5a - 10b + 3c$ ?

EXAMPLE 4. 
$$\frac{1}{\sqrt{2} + \sqrt{3}} = \frac{1}{\sqrt{2} + \sqrt{3}} \cdot \frac{\sqrt{4} - \sqrt{6} + \sqrt{9}}{\sqrt{4} - \sqrt{6} + \sqrt{9}} = \frac{\sqrt{4} - \sqrt{6} + \sqrt{9}}{5}$$

Solve  $\sqrt{3x-5} + \sqrt{2x+3} + 1 = 0$ .



FIGURE 3

This example shows possible modification of items to explicitly show gaps.

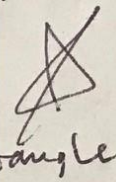
The picture shows John's attempt to cover a rectangle with equal parts to measure the area. John says that he used 7 unit squares to cover the shape so the area is 7 unit squares.



- Is John correct? Explain.
- It looks like John has some gaps, or uncovered spaces, in his picture. What would the area of the rectangle be if he did not have any gaps?
- Was John's area too big or too small? Why do you think that is?

Previous studies have shown that even with pictured squares, rows, and columns, the connection between counting unit squares and area is unclear to elementary school students (Battista 2004). With limited opportunities to understand array structure, students may struggle to see how the two are related (Saxe & Taylor 2004).

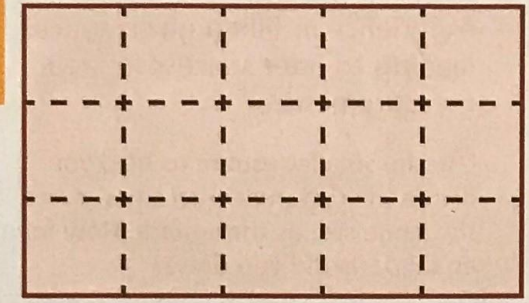
*measure the area of a rectangle.*



*rectangle*  
*instead of this,*  
*do all the parts all on overlaps*  
*(any gaps or holes; why overlaps are bad).*  
*Relate to length.*

FIGURE 4

This possible modification explicitly shows row and column structure.



1. How many rows and columns are in this rectangle? \_\_\_
- 2a How many unit squares can be placed in each row ~~and column?~~
- 2b ~~How many unit squares can be placed in each column?~~
3. There are \_\_\_ rows, with \_\_\_ squares in each row.
4. There are \_\_\_ columns, with \_\_\_ squares in each row
5. Use skip counting in two different ways to find out how many total squares fit in the shape. \_\_\_
6. How many unit squares are needed to cover this rectangle without any gaps or overlaps? \_\_\_ Explain how you know.



## 6.2 Unit Rate

In the previous section, we defined what an average or average rate is. Let's look at how the concept of a unit rate can help us make better decisions.

### CLASS ACTIVITY 2

**Objective:** To compare various quantities using different units.

Two pens of different areas, each containing different numbers of puppies, are shown below. Which pen is more crowded?



Pen A



Pen B

	Area (m <sup>2</sup> )	Number of Puppies
Pen A	5	8
Pen B	8	10

#### Questions

- Which puppy pen do you think is more crowded and why?
- Next, compare them by finding the number of square meters per puppy.

Pen A    8 puppies →  m<sup>2</sup>

1 puppy →  $\frac{\text{input}}{8} = \text{input} \text{ m}^2$

There is  m<sup>2</sup> for each puppy.

Pen B    10 puppies →  m<sup>2</sup>

1 puppy →  $\frac{\text{input}}{10} = \text{input} \text{ m}^2$

There is  m<sup>2</sup> for each puppy.

Based on this method, which pen is more crowded and why?



Pen A



Pen B

	Area (m <sup>2</sup> )	Number of Puppies
Pen A	5	8
Pen B	8	10

#### Questions

Which puppy pen do you think is more crowded and why?

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4. Complete the table by using the reciprocal of the divisors to write equivalent multiplication expressions.

Division Expression	Quotient	Equivalent Multiplication Expression	Product
$6 \div 3$	2	$6 \times \frac{1}{3}$	2
$6 \div 2$			
$6 \div \frac{3}{2}$			
$6 \div 1$			
$6 \div \frac{1}{2}$			
$6 \div \frac{1}{3}$			

- (a) Look at the patterns in the divisors and the quotients. What happens to the quotient, as the divisor gets smaller?
- (b) What do you notice about the quotients of the division expressions and the products of the equivalent multiplication expressions?

4/7/2020

A unit square has one vertex at the center of another unit square. What is the area of overlap?

# How Moisture in the Air Brings on the Heat



When the sun radiates blistering heat, how hot the air feels depends on how much moisture is in it.

Ninety degrees Fahrenheit could pass for an unpleasant 100 degrees or a dangerous 132.

Meteorologists call this the heat index, a value that combines the effects of air temperature and relative humidity to represent the perceived temperature. The index is derived from a mathematical equation that accounts for everything from

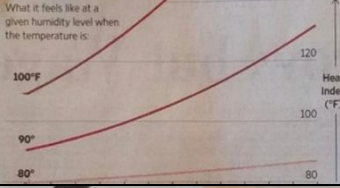
This year, more than a dozen deaths are believed to be heat-related in the Phoenix area, which was so hot last month that airlines grounded more than 40 flights.

Each of the National Weather Service's 122 offices issues alerts at its own discretion, but in general, an advisory is issued if within 12 hours the heat-index temperature is expected to hit 100 degrees Fahrenheit and last for at least two days. A warning is issued if in the same period the index is expected to hit at least 105 degrees.

When the body gets

## Turning Up the Heat

The Heat Index is derived from a mathematical equation that uses temperature and humidity, and incorporates factors including body size, to come up with what the temperature feels like.



familiar measurement is dew point, the temperature below which water vapor begins to condense, forming dew, fog or raindrops.

"If the dew point is in the 60s in the summer, it's a little humid," Mr. Jacks said. "If it gets into the upper 60s, it's pretty bad. In the 70s, it's really oppressive."

The heat index, which the National Weather Service has used since 1979, is based on the work of R.G. Steadman, a professor in the textiles and clothing department of Colorado State University in Fort Collins who created a chart of val-

$$.22475541 * T * RH - .00683783 * T * T - .05481717 * RH * RH + .00122874 * T * T * RH + .00085282 * T * RH * RH - .00000199 * T * T * RH * RH$$

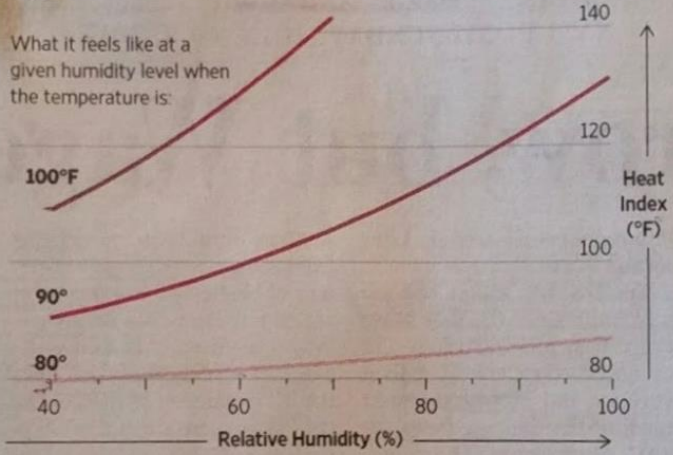
The equation is valid for temperatures ranging from 80 to 110 degrees Fahrenheit and humidity ranging from 40% to 100%.

But the index, once calculated, is not one-size-fits-all. It applies to someone who is 5 feet, 7 inches tall, weighs 147 pounds, is wearing long trousers and a short-sleeved

dozen be phen last ounded offices dis- an ad- in 12 temper- 100 last warn- ame ected ees. gets and pira- ies r is

## Turning Up the Heat

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Source: National Weather Service

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Mr. Steadman's calculations, which incorporated about 20 different variable

$$.22475541 * T * RH - .00683783 * T * T - .05481717 * RH * RH + .00122874 * T * T * RH + .00085282 * T * RH * RH - .00000199 * T * T * RH * RH$$

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The equation is valid for temperatures ranging from 80 to 110 degrees Fahrenheit and humidity ranging from 40% to 100%.

Ole M To Re Camp Build

By Mizana M... The Union will remain building... A former American... white sup... The sc... with how history modern... After a celor's A History... said This move th... Vardam known... Acco... school... man, a served from 13 sented Senate "disting... The Vardam... A sc... Jam... was... unar...





Place the clock hands so the sum of the numbers on one side of them equals the sum on the other side.

MUS



5

(included)

EESE  
CHILI



9

2 oz.  
cont.

ies

OGURT



7

All Natural  
**LAND O LAKES  
LARGE BROWN EGGS**



**2/\$5**  
12 ct.  
pkgs.

Salted or Unsalted  
**BREAKSTONE'S  
BUTTER QUARTERS**



**\$4.99**  
16 oz.  
pkg.

Assorted Varieties  
**GALBANI  
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Assorted Varieties  
**GALBANI  
RICOTTA CHEESE**



**\$4.99**  
32 oz.  
cont.

**BREAKSTONE'S  
TEMP-TEE  
WHIPPED  
CREAM CHEESE**



**\$3.99**  
11.5 oz.  
cont.

Assorted Varieties  
**DAISY SOUR CREAM**



**2/\$4**  
16 oz.  
conts.

GRANULATED  
**JACK  
FROST  
SUGAR**



**\$1.99**  
1 lb.  
bag

Assorted Varieties  
**GENOVA TUNA**



**2/\$4**  
5 oz.  
cans

**ICY POINT  
PINK SALMON**



**2/\$5**  
14.75 oz.  
cans

**BOTTICELLI  
OLIVE OIL**



**\$9.99**  
50.7 oz.  
btl.

**HUNT'S  
TOMATO  
KETCHUP**



**99¢**  
24 oz.  
btl.

Assorted Varieties  
**JIF  
PEANUT BUTTER**



**\$2.99**  
16 oz.  
cont.

12-24

Charm

Ultra Soft

5

POLAND



25

5

Ass

AN



7



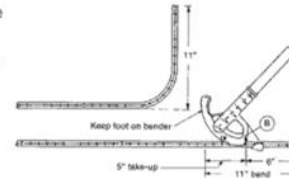
## Conduit Bending Instructions (EMT Bender)

### Accurate Stubs

Subtract take-up from desired stub height. This gives distance at which to place B on bender from the end of the tube. To make 11", 90° bend with 1/2" tube, allow for 5" for take-up as shown on diagram.

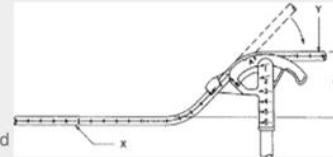
With 3/4" tube, allow 6"

With 1" tube, allow 8"



### True Offsets

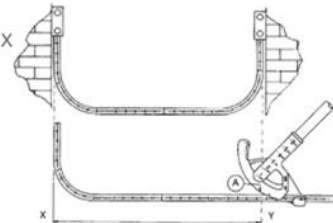
Line up arrow on either side of hook with guideline and make 45° bend in tube. Reverse tube in bender and adjust so that X is lined up with inch-mark on bender corresponding to depth of offset desired. Line up guideline with opposite arrow and make second 45° bend. A true offset, in the same plane, will result between X and Y.



### Back-to-Back Bends

Make stub bend at X with guide-line centered on either arrow located on side of hook. Measure distances from X to Y on tube.

Reverse bender and put A on bender at Y on tube. Line up guide-line with opposite arrow than used when making first stub and make second bend.

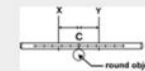


### Saddle Bends

C -- Center of finished Saddle Bend

X -- Double of the diameter of round object from C

Y -- Double of the diameter of round object from C



### Saddle Bend, Step 1

Place tube in bender so that "C" on tube is at notch on bender and make a 45° bend. (A 45° bend is reached when bender handle is at a right angle to the tube.)



# Agenda

Introduction

The game of “Good Thing, Bad Thing, Change One Thing”

Some ways to make improvements

**Q&A Session**

Next steps

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Questions for Our Guests?

# Agenda

Introduction

The game of “Good Thing, Bad Thing, Change One Thing”

Some ways to make improvements

Q&A Session

**Next steps**

# How you can carry the work forward

- Read [the 4H article](#)
- Evaluate [Algebra by Example](#)
- Start a math problem notebook/scrapbook
- When evaluating an assignment, try doing “Good Thing, Bad Thing, Change One Thing”
- Find a colleague to trade assignments – offer each other a good thing/bad thing/change one thing
  
- Tweet or email us before-and-after photos of an assignment – tell us if your changes helped!
- Tweet or email us an assignment, and we’ll suggest a “Good Thing, Bad Thing, Change One Thing”

#MathFixerUpper

Email us at [info@studentsachieve.net](mailto:info@studentsachieve.net).

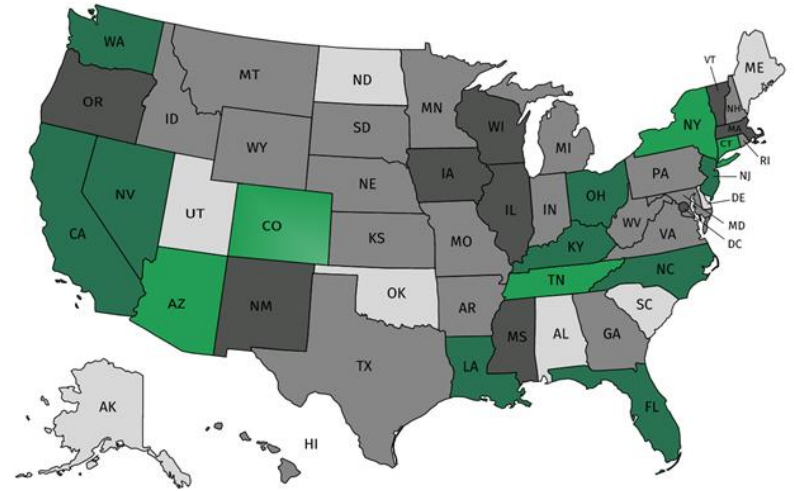
Resource Name	Link
Join Our Network!	<a href="http://www.achievethecore.org/ca-signup">www.achievethecore.org/ca-signup</a>
Matthews, On Mindset and Practices for Re-Integrating “Belonging” into Mathematics Instruction	<a href="http://www.teachingworks.org/images/files/TeachingWorks_Matthews.pdf">http://www.teachingworks.org/images/files/TeachingWorks_Matthews.pdf</a>
Algebra By Example	<a href="https://www.serpoinstitute.org/algebra-by-example">https://www.serpoinstitute.org/algebra-by-example</a>
Coherence Map	<a href="https://achievethecore.org/coherence-map/HS/M/tasks">https://achievethecore.org/coherence-map/HS/M/tasks</a>
Widely Applicable Prerequisites for College and Careers	<a href="https://achievethecore.org/page/701/widely-applicable-prerequisites-for-college-and-careers">https://achievethecore.org/page/701/widely-applicable-prerequisites-for-college-and-careers</a>
“How I See Addition Facts”	<a href="http://static1.squarespace.com/static/54f60ba7e4b0625e8c527330/t/57c79dad03596e87a7a0705a/1472699830328/CMT-Fall+2016k.pdf">http://static1.squarespace.com/static/54f60ba7e4b0625e8c527330/t/57c79dad03596e87a7a0705a/1472699830328/CMT-Fall+2016k.pdf</a>



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# Please Join Us Again Next Month!

- Next month's webinar:  
**Reading, Learning, Growing: Creative Ideas to Build Knowledge and Support Literacy Across Subjects**
- **June 3, 2020 @7 P.M. ET**

Register Here:

<https://event.on24.com/wcc/r/2272340/730BDB5943A462A0A7D531C751AECF4B>

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Thank You!